Representations of affine and vertex operator algebras Ten-minutes problem 5

Prove that the central extension of the Witt algebra defined by

$$
\left[L_{n}, L_{m}\right]=(n-m) L_{n+m}+c \delta_{n,-m} n^{3}
$$

is nontrivial.

