Representations of affine and vertex operator algebras Ten-minutes problem 7

Compute the image of the polynomial $z^3(2x_1^2 + x_2)$ under the boson-fermion correspondence.