## Affine Kac-Moody Lie algebras Ten-minutes problem 2

Prove that diagonal matrices form a maximal commutative subalgebra of  $\mathfrak{sl}_n$ . Does there exist another commutative subalgebra of  $\mathfrak{sl}_n$  of the same dimension? Does there exist a commutative subalgebra of larger dimension?