

Course Title (in English) Gauge fields and complex geometry

Course Title (in Russian) Калибровочные поля и комплексная геометрия

Lead Instructor(s) Rosly, Alexei

Status of this Syllabus The syllabus is a final draft waiting for form approval

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1. Annotation

1. Self-duality equations, Bogomolny equations.

2. Relation to holomorphic bundles.

- 3. Relation to holomorphic bundles on twistor space.
- 4. Conformal symmetry and complex geometry in twistor space.
- 5. Elements of superfield formulation of SUSY field theories.
- 6. Chirality type constraints and complex geometry.
- 7. Some examples of superfield theories which require complex geometry.
- 8. BPS conditions in SUSY theories and complex geometry.
- 9. Elements of Hitchin's integrable systems and related complex geometry.

Course Prerequisites

Course Description

Student should be familiar with classical mechanics and classical field theory (Landau-Lifshitz' Vol 1 and 2), calculus, and basic differential geometry.

2. Structure and Content

Course Academic Level

Master-level course suitable for PhD students

Number of ECTS credits

6

| Topic | Summary of Topic | Lectures (# of hours) | Seminars (# of hours) | Labs (# of hours) |
|-----------------|--------------------------------------|-----------------------|-----------------------|----------------------|
| Gauge Theory | Mathematical aspects of Gauge Theory | 1.5 h | 0 | 0 |

3. Assignments

4. Grading

| Type of Assessment | Graded | | |
|--------------------|---------------|--------------------|--|
| Grade Structure | Activity Type | Activity weight, % | |
| | Final Exam | 100 | |
| A: | Grading Scale | | |
| B: | 86 | | |
| C: | 76 | | |
| D: | 66 | | |
| E: | 56 | | |

5. Basic Information

F:

0

| Attendance Requirements | Optional | | |
|---|--|--------------|--|
| Course Stream | Science, Technology and Engineering (STE) | | |
| Course Delivery Frequency | Every year | | |
| | | | |
| Students of Which Programs do | Masters Programs | PhD Programs | |
| Students of Which Programs do You Recommend to Consider this Course as an Elective? | Masters Programs Mathematical and Theoretical Physics | PhD Programs | |
| You Recommend to Consider | Widotolo i Togranio | PhD Programs | |

6. Textbooks and Internet Resources

| Required Textbooks | ISBN-13 (or ISBN- 10) |
|--|--------------------------|
| Landau LD, Lifshitz EM. The Classical Theory of Fields. Vol. 2 (4th ed.). Butterworth-Heinemann, 1975. | 978-0-7506-2768-9 |

| Recommended Textbooks | ISBN-13 (or ISBN-10) |
|---|-------------------------|
| Green, M. B.; Schwarz, J. H.; Witten, E., Superstring Theory. Vol. 2: Loop amplitudes, anomalies and phenomenology. Cambridge etc., Cambridge University Press 1987. XII, 596 pp. | 0 521 32999 X |
| Becker K, Becker M, Schwarz JH. String Theory and M-Theory: A Modern Introduction. Cambridge University Press, 2006. | 9780521860697 |
| Nakahara M. Geometry, Topology and Physics, 2nd Edition. IOP Publishing Ltd 2003. | 9780750306065 |
| Hitchin NJ, Segal GB, Ward RS. Integrable Systems: Twistors, Loop Groups, and Riemann Surfaces. Oxford University Press, 1999. | 0198504217 |
| Atiyah M. Geometry of Yang-Mills fields. Edizioni della Normale, 2013 | 8876423036 |
| Атья М. Геометрия и физика узлов. Мир, 1995. | 5-03-002892-7 |
| Грин М., Шварц Дж., Виттен Э. Теория суперструн, том 2. Мир, 1990. | 5-03-001567-1 |

7. Facilities

8. Learning Outcomes

Knowledge

Basic constructions and theorems in complex geometry which are widely used in modern field theory.

Skill

Understanding of mathematical terminology encountered in modern theoretical physics papers. Some know-how in exploiting complex geometry in field theory.

Experience

Solving problems in classical field theory which are most characteristic and basic for modern theoretical physics.

Do you want to specify outcomes in another framework?

Knowledge-Skill-Experience is good enough

9. Assessment Criteria

Select Assignment 1 Type

Final Exam

Or Upload Example(s) of Assignment 1

https://ucarecdn.com/a0ef7a9e-e91a-4979-973e-b1c65b23d566/

Assessment Criteria for Assignment 1

Solving problems on day of exam. Activity during the semester.

10. Additional Notes

Free Style Comments (if any)

Examples of problems given above come from the last year. Their topics not always coincide with the present year's course. Nevertheless, students are encouraged to solve them also and this will count for the final assessment. New problems will appear in the lectures. Presenting solutions during the semester is particularly welcomed.