Darboux coordinates for symplectic groupoid

We explain construction of Darboux coordinates for generic symplectic leaves of the groupoid of unipotent upper triangular matrices using Fock-Goncharov coordinates for framed moduli space of flat connections and express the braid group action as a sequence of cluster mutations.

This is a joint project with L.Chekhov.